# QRULE

## A COMPUTER PROGRAM FOR LANDSCAPE HYPOTHESIS TESTING

# developed by

# Robert H. Gardner Appalachian Laboratory University of Maryland Center for Environmental Science Frostburg, MD 21532

QRULE is an extension of RULE (Gardner 1999), a program for scale-dependent analysis of landscape patterns. The extensions provided in QRULE are designed to assist the user in the development and testing of alternative hypotheses relating the process of landscape change to the patterns observed. These differences may be statistically compared with a simple random pattern (i.e., the classical neutral model of Gardner et al. 1987), against an new model within QRULE, or by alternative models developed by the user.

This document provides a brief overview, focusing on the new features in QRULE. It is assumed that the reader has experience using RULE and is familiar with the concepts of neutral landscape models (Turner et al. 2001).

Program documentation, example input and output files, and the source code for QRULE may be obtained from <u>www.al.umces.edu/QRULE</u>. The Open Software License (<u>http://www.opensource.org/licenses/index.php</u>) applies to the distribution, use, and possible alteration of QRULE.

## **OVERVIEW OF IMPROVEMENTS AND ADDITIONS**

- 1. The output files generated by QRULE have been extensively revised and reformatted to assist in data display and statistical comparisons (see Table 1). Two new files, *assmat.dat* and *arcgrid.map* have been added. The association matrix among map cover types is statistically evaluated in *assmat.dat*, while *arcgrid.map* formats the first map iteration for display in ArcInfo.
- 2. The pattern metrics produced from map analysis are now expressed in metric units (i.e., in meters, hectares, etc.).
- 3. It is now possible, using the *patch\_cfd.dat* data file to directly display the cumulative frequency distribution of patch sizes for each land-cover class. A program written in PERL is provided (cfdsum.pl) to illustrate how these plots may be performed.
- 4. The addition of alternative neutral models to QRULE is illustrated with the "mask" <X> option. This model is designed to test the hypothesis that landscape pattern is largely determined by dominant features (e.g., rivers, lakes, urban development) that constrain the patterns of other cover types. Adding additional options to QRULE is not difficult, but requires familiarity with Fortran 95 and the availability of a suitable compiler.

#### **RUNNING QRULE**

Input to QRULE may be either interactive or via file redirection. Each execution of QRULE requires the specification of: 1) the type of map to be generated and/or analyzed; 2) map characteristics; and 3) the output desired. Two types of input requests are illustrated below. The first is to analyze an existing map, while the second is to use the "masked" model for hypothesis testing. Blue text indicates output from QRULE while black text indicates user response.

#### First example: Analyze an input map

```
Orule (v 4.1) Landscape Pattern Analysis
                                                           08/01/05
         Enter map type to be analyzed:
               <I>> Input existing map file
               <R> Generate a random map (with replacement)
               <S> Generate a simple random map
               <M> Generate a multifractal random map
               <G> Generate a multifractal random map with a gradient
               <X> Use input map as mask, random map for neutral model
i
         Map choice: I
         Enter name of input map file
rocr reclass.map
         Input map name: rocr reclass.map
         Enter number of map rows and columns (max = 2048 ea.)
512 512
         Rows x Columns =
                             512 x
                                      512
         Enter the number of map classes
4
         Map classes =
                          4
         Enter the neighborhood rule
               1 - \text{nearest neighbor} (N nb = 4)
               2 - next nearest neighbor (N nb = 8)
               3 - 3rd nearest neighbor (N nb = 12)
               4 - user defined
1
         Rule choice is: 1
         Enter the number of replications
1
         N Reps =
                      1
         Create an output maps?
            N = None
            G = generated map
            S = cluster Size map
            C = cluster ID map
n
         Map output choice = N
```

Appendix A gives the results of this example in the 'rulerun.log' file.

#### Second Example: Use the "mask" neutral model

This example requires two maps. The first map will be used to extract the land-cover adjacency matrix used in the neutral model. Bracketed text (in italics) has been inserted to clarify the purpose of some of the responses.

```
Qrule (v 4.1) Landscape Pattern Analysis 08/01/05
        Enter map type to be analyzed:
              <I>> Input existing map file
              <R> Generate a random map (with replacement)
              <S> Generate a simple random map
              <M> Generate a multifractal random map
              <G> Generate a multifractal random map with a gradient
              <X> Use input map as mask, random map for neutral model
х
        Map choice: X
        Enter number of map rows and columns (max = 2048 ea.)
512 512
        Rows x Columns = 512 x
                                    512
        Enter name of file to be used as a mask
rocr reclass.map
         Input map name: rocr reclass.map
        Enter number of cover types of the mask map
4
        Enter number of cover types for random generated maps
3
           {reclassification will be necessary}
        Cover types: mask = 4 random =
             Reclassify masked map
             Cover type 0 becomes ...
           {the '0' class is a non-cover type - e.g., roads, etc.}
0
             Cover type
                         1 becomes ...
1
             Cover type
                        2 becomes ...
2
             Cover type 3 becomes ...
```

```
Cover type
                         4 becomes ...
            {class '4' has been set to class '0'}
0
         from --> to
                0
             0
             1
                 1
             2
                 2
             3
                 3
             4
                 0
         Type in the habitat type for the matrix
           set to zero to automatically select
1
           { '1' is agriculture}
         Background (matrix) = 1
         Now we need the parameters for the
         random map cover types
         Enter a negative random number seed
-1918171
         Random number seed: -1918171
         Enter the neighborhood rule
               1 - \text{nearest neighbor} (N nb = 4)
               2 - \text{next nearest neighbor} (N nb = 8)
               3 - 3rd nearest neighbor (N_n = 12)
               4 - user defined
1
         Rule choice is: 1
         Map classes = 3
         Enter the 4 probabilities, starting with p(0)
0
0.79955
0.19029
0.01015
         The normalized probabilities are:
                           CumP
                Р
               0.0000
           0
                          0.0000
                         0.7996
               0.7996
           1
               0.1903
           2
                          0.9898
               0.0102
                          1.0000
           3
         Enter the number of replications
12
         N Reps =
                    12
         Create an output maps?
            N = None
            G = generated map
            S = cluster Size map
            C = cluster ID map
g
         Map output choice = G
         Name of output file?
scratch.map
```

3

```
4
```

```
Output file for generated map: scratch.map

Perform map analysis?

 <N>o analysis

 <L>acunarity analysis

 <R>ule analysis

 <A>ll (both Rule and Lacunarity)

r
Analysis method: RULE
What is the resolution of each grid element?

(length of the side of a grid element, in meters)
30
.....
```

See Appendix B for a listing of the entire input-output stream for this example.

## File redirection for batch-mode execution

Analysis projects often require multiple executions of QRULE. In these cases it will be convenient to use file redirection for input and output. In addition, the files produced by QRULE (Table X) will need to be renamed in order to prevent them from being overwritten (and thus destroyed) by subsequent program execution. If all the input responses are prepackaged in an input file (i.e., *name.scriptfile*) then QRULE can be run with a single line typed at the command prompt:

Qrule < *name.scriptfile* > *output.save* 

Where 'QRULE' executes the program, the '<' causes QRULE to read input from *name.scriptfile* and the '>' causes screen output to be redirected to a file called *output.save*. Of course *name.scriptfile* and *output.save* are optional names for the files of your choice. Subsequent to execution, *rulerun.log* should be renamed to save the results and *patch\_cfd.dat* renamed if summary statistics of patch sizes are desired.

Of course, multiple runs can be packaged into a batch file allowing unattended execution of multiple maps. This is most useful when the size maps and number of iterations are large.

File name <sup>1</sup>	Unit	Туре	General description of contents
rulerun.log	10	G	log file of program input and simulation results
patch_cfd.dat	11	G	patch size frequency distribution for each map and habitat type. Output includes mean patch size, edge, radius mean square, and fractal for each patch size.
'Idfile'	12	G	output map with each patch uniquely identified
'sizefile'	13	G	name of output map with the patch sizes uniquely labeled
'outfile'	14	G	name of output map with habitat types uniquely labeled
'mapfile'	15	Ι	name of input map file for analysis by RULE
assmat.dat	16	G	matrix of neighbor association frequencies for each map
arcgrid.map	19	G	single map with header for input to ArcGrid for visualization and display
lacun.dat	20	G	output of lacunarity results

Table 1. ASCII files that are used (I) or generated (G) by QRULE

<sup>1</sup> Single quoted names are specified by the user at runtime. Non-quoted names are invariant, being produced by each use of QRULE. The non-quoted file names should be renamed following each execution of QRULE to preserve program results.

Example input and output files are available at www.al.umces.edu/Qrule

## ADDITIONAL FILES FOR PROCESSING DATA

The philosophy of the UNIX and LINUX operating systems is to increase programming efficiencies by linking programs with existing utilities via input-output files. Many of the statistical analyses that we have performed were accomplished by using existing plotting and statistical analysis software. Three PERL scripts, cfdsum.pl, compare.pl, and Qrule.pl, and a single fortran program, Kstest.f90, are provided (see otherstuff.zip) to aid the user in analyzing the output from QRULE. These files and programs are not documented here, but are offered to those with sufficient expertise to use and adapt to individual needs.

#### SOURCE CODE OVERVIEW

The list of files required to compile QRULE, and the Makefile used to do so, are given in Table 2. Because QRULE uses advance features of Fortran 95, the Lahey compiler was used for both the DOS and LINUX versions (Lahey Computer Systems 1999). Most of the files listed in Table 2 contain multiple subroutines that are closely related to the functions listed.

#### Table 2 Program files for compilation and execution of QRULE

File Name	File Type	Purpose
Makefile	make	recompile and update Fortran executable
Rule	Executable	
Qrule	Fortran executable	Available for DOS (Qrule.exe) and LINUX operating systems
	Fortran 95 So	urce Code
genmap.f90	Subroutines for map	generation
hfract.f90	Multifractal map rou	utine
input.f90	Program input and co	ontrol
lacun.f90	Subroutine for optic analysis (Plotnick e	onal output of lacunarity et al. 1993).
main.f90	Routine governing p	rogram execution
mapanal.f90	Routines for map and	alysis
module.f90	Defines variables an	nd sets their dimensions
patchid.f90	Routines for identi:	fication of landscape patches
ran1.f90	Random number genera Receipes (Press et a	ation routine from Numerical al. 1992)
sizeit.f90	Subroutines control: map variables	ling the dynamic dimension of
stats.f90	Calculation and outp indices	put of map statistics and

Additional neutral models may be added to QRULE by:

- 1. Revising the input routine to accept the option of executing a different (additional) neutral model. The variable 'maptype' is used to identify the type of neutral model to generate. Code similar to that for the other map types will need to be added to this input file to recognize this new options and the parameters it may require.
- 2. The subroutine for the new neutral model should be added to the genmap.f90 file. In addition a call must be added to the GenMap routine (under 'select case (maptype)') in order for this new model to be linked with the QRULE code.
- 3. Recompile using Makefile

Obviously, the above is only an outline of the changes which may be required. Familiarity with fortran – or the ability to link programs written in other languages with this fortran code – are a prerequisite for making changes to QRULE.

## METRICS AND STATISTICS PRODUCED BY QRULE

QRULE provides a set of landscape metrics that have proven to be helpful in understanding the effect of landscape fragmentation on pattern generation (Gardner 1999). Additional analyses may be achieved by exporting maps to ArcView or other programs such as Fragstats (McGarigal et al. 2002).

One new statistic has been added to QRULE: a chi-square test of the matrix of association of land-cover types. 'Chisquare', the subroutine performing this analysis, may be found in the file 'mapanalysis.f90.' There were 4 cover types in the examples listed in the appendices, with an association matrix that formed a 4 x 4 chisquare contingency table with 9 degrees of freedom (Zar 1996). The association matrix is listed in the examples in Appendix A and B includes the '0' cover class –regarded by QRULE as a "no data" class. Although these frequencies are listed, they were not a part of the chisquare test.

#### Appendix A: Log file for first example

```
Qrule (v 4.1) Landscape Pattern Analysis
                                                                                                                          08/01/05
                   Map choice: I
                   Input map name: rocr reclass.map
                   Rows x Columns = 512 x 512
                   Map classes = 4
                   Rule choice is: 1
                   N Reps = 1
                   Map output choice = N
                   Analysis method: RULE
                   Resolution: 30.0000
                                                                   meters
                                                  Mean Association Matrix
                   Avg_ChiX = 890910. w/ 9 df (%Xceed = 100.0000)
0 1 2 3 4
                          0 0.034900 0.001690 0.000614 0.000413 0.001469
                          1 0.001690 0.204405 0.008997 0.000947 0.063994
                          2 0.000614 0.008997 0.037996 0.000063 0.018968
                          3 0.000413 0.000947 0.000063 0.001538 0.000593
                          4 0.001469 0.063994 0.018968 0.000593 0.525662
                   p's 0.039086 0.280034 0.066639 0.003555 0.610686
                   STATISTICAL SUMMARY (N=
                                                                           1; Resolution= 30.0000 meters)
--Cover Type 0 (non habitat)-- [p = 0.0391 Cum. p = 0.0391]

--Land Cover Type 1-- [p = 0.2800 Cum. p = 0.3191]

Variable Units Mean St.Dev. C. V. Minimum
 --Land Cover Type 1--[p =0.2800Cum. p =0.3191]Variable Units MeanSt.Dev.C. V.MinimumMaximumL.C.size ha1152.450.000000.000001152.451152.45L.C.edge m238320.0.000000.00000238320.238320.L.C.fract -1.691010.000000.000001.691011.69101L.C.rms m2974.930.000000.000002974.932974.93TTL clstr N5420.000.000000.000005420.005420.00TTL edgs m0.238968E+070.000000.000000.238968E+070.238968E+07Sav size ha495.7110.000000.00000495.711495.711S_Freq N73393.00.000000.0000073393.073393.0Cor_len m2538.970.000000.000000.000000.00000Perc< %</td>0.000000.000000.000000.000000.00000
--Land Cover Type 2--<br/>Variable Units Mean[p = 0.0667Cum. p = 0.3858]L.C.size ha 88.5600St.Dev.C. V.MinimumMaximumL.C.edge m 27780.00.000000.0000027780.027780.0L.C.fract - 1.744170.000000.000001.744171.74417L.C._rms m 570.2100.000000.00000570.210570.210TTL clstr N 3349.000.000000.000003349.003349.00TTL edgs m 905160.0.000000.0000014.885914.8859S_Freq N 17484.00.000000.0000017484.017484.0Cor_len m 435.8730.000000.00000435.873435.873Perc% 0.000000.000000.000000.000000.00000
--Land Cover Type 3--[p = 0.0036Cum. p = 0.3893]Variable Units MeanSt.Dev.C. V.MinimumL.C.size ha 6.930000.000000.000006.93000L.C.edge m 2400.000.000000.000002400.00L.C.fract - 1.517650.000000.000001.51765
```

L.C. rms	m	204.194	0.00000	0.00000	204.194	204.194
TTL clstr	Ν	345.000	0.00000	0.00000	345.000	345.000
TTL edgs	m	63780.0	0.00000	0.00000	63780.0	63780.0
Sav size	ha	2.26522	0.00000	0.00000	2.26522	2.26522
S Freq	Ν	934.000	0.00000	0.00000	934.000	934.000
Cor_len	m	169.501	0.00000	0.00000	169.501	169.501
Perc	00	0.00000	0.00000	0.00000	0.00000	0.00000
Land Cove	er T	ype 4	[p =	0.6107	Cum. $p = 1.0000$ ]	
Variable 1	Unit	s Mean	St.Dev.	C. V.	Minimum	Maximum
L.C.size	ha	10208.3	0.00000	0.00000	10208.3	10208.3
L.C.edge	m	0.136008E+07	0.00000	0.00000	0.136008E+07	0.136008E+07
L.C.fract	-	1.87103	0.00000	0.00000	1.87103	1.87103
L.Crms	m	5419.64	0.00000	0.00000	5419.64	5419.64
TTL clstr	Ν	2817.00	0.00000	0.00000	2817.00	2817.00
TTL edgs	m	0.270660E+07	0.00000	0.00000	0.270660E+07	0.270660E+07
Sav size	ha	7656.26	0.00000	0.00000	7656.26	7656.26
S_Freq	Ν	160085.	0.00000	0.00000	160085.	160085.
Cor_len	m	5303.52	0.00000	0.00000	5303.52	5303.52
Perc	00	1.00000	0.00000	0.00000	1.00000	1.00000

#### Appendix B: Log file for second example

```
Qrule (v 4.1) Landscape Pattern Analysis
                                                                                           08/01/05
                Map choice: X
                Rows x Columns =
                                                512 x
                                                                512
                File to use as mask: rocr reclass.map
                Cover types: mask = 4 random = 3
                from --> to
                       0 0
                       1
                              1
                       2
                             2
                       З
                             3
                       4
                               0
                Random number seed: -1918171
                Rule choice is: 1
                Map classes = 3
                The normalized probabilities are:
                                       CumP
                            Ρ

        0
        0.0000
        0.0000

        1
        0.7996
        0.7996

        2
        0.1903
        0.9898

        3
        0.0102
        1.0000

                N Reps = 12
                Map output choice = G
                Output file for generated map: scratch.map
                Analysis method: RULE
                Resolution: 30.0000 meters
                Using mask with ***** sites [p(0) = 0.64977]
                                         Mean Association Matrix
                Avg_ChiX = 875462. w/ 5 df (%Xceed = 100.0000)
0 1 2 3
                      0 0.563500 0.083590 0.002552 0.000131
                     1 0.083590 0.174154 0.020895 0.001571
                     2 0.002552 0.020895 0.041427 0.001596
                      3 0.000131 0.001571 0.001596 0.000249
                p's 0.649772 0.280210 0.066471 0.003547
                STATISTICAL SUMMARY (N= 12; Resolution= 30.0000 meters)
--Cover Type 0 (non habitat)-- [p = 0.6498 Cum. p = 0.6498]
--Cover Type 0 (non naz----)

--Land Cover Type 1-- [p = 0.2802 Cum. p = 0.9500]

Variable Units Mean St.Dev. C. V. Minimum Maximum

L.C.size ha 584.370 127.073 21.7453 360.810 785.340

151230 46130.3 30.5034 95940.0 270300.

1 77512
 JariableUnitsMeanSt.Dev.C. V.L.C.sizeha584.370127.07321.7453L.C.edgem151230.46130.330.5034L.C.fract-1.716800.463942E-012.70237L.C._rmsm1716.60411.68523.9826TTL clstrN7315.1756.00620.765618

        Alfinition
        Addition

        360.810
        785.340

        95940.0
        270300.

        1.63812
        1.77512

        1086.09
        2777.87

        7232.00
        7410.00

 III CISCL N/315.1/56.00620.7656187232.007410.00TTL edgs m0.334782E+0713571.60.4053840.331752E+070.3376381Sav size ha123.54628.087922.734780.3961184.840S_Freq N73462.97.044770.958956E-0273450.073474.0Cor_len m1439.29346.31124.0612916.1642255.83Perc%0.000000.000000.000000.00000
                                                                    0.765618
                                                                                        0.331752E+07 0.337638E+07
80.3961 184.840
--Land Cover Type 2--[p = 0.0664Cum. p = 0.9965]Variable Units MeanSt.Dev.C. V.MinimumMaximumL.C.size ha 56.947510.401718.265444.010076.6800L.C.edge m 18510.03574.7819.312712960.024780.0
```

L.C.fract	-	1.68404	0.411394E-01	2.44290	1.63345	1.79039
L.C. rms	m	497.870	52.2798	10.5007	382.026	580.443
TTL clstr	Ν	2219.58	81.1631	3.65668	2083.00	2403.00
TTL edgs	m	789545.	16484.5	2.08784	758760.	831240.
Sav size	ha	14.8172	1.48497	10.0220	12.3929	17.9630
S Freq	Ν	17418.2	5.00227	0.287186E	2-01 17409.0	17431.0
Cor len	m	381.128	37.5106	9.84202	312.358	444.973
Perc	00	0.00000	0.0000	0.00000	0.00000	0.00000
Land Cove	er T	'vpe 3	= q]	0.0035	$C_{11}m$ , $p = 1.00001$	
		100 0	L 1-			
Variable (	Jnit	s Mean	St.Dev.	C. V.	Minimum	Maximum
Variable U L.C.size	Jnit ha	.s Mean 0.562500	St.Dev. 0.115925	C. V. 20.6089	Minimum 0.450000	Maximum 0.810000
Variable U L.C.size L.C.edge	Jnit ha m	Mean 0.562500 405.000	St.Dev. 0.115925 81.4081	C. V. 20.6089 20.1008	Minimum 0.450000 300.000	Maximum 0.810000 600.000
Variable U L.C.size L.C.edge L.C.fract	Jnit ha m -	Mean 0.562500 405.000 1.57308	St.Dev. 0.115925 81.4081 0.103942	C. V. 20.6089 20.1008 6.60753	Minimum 0.450000 300.000 1.40368	Maximum 0.810000 600.000 1.75647
Variable U L.C.size L.C.edge L.C.fract L.Crms	Jnit ha m - m	s Mean 0.562500 405.000 1.57308 59.4908	St.Dev. 0.115925 81.4081 0.103942 5.77370	C. V. 20.6089 20.1008 6.60753 9.70520	Minimum 0.450000 300.000 1.40368 50.9117	Maximum 0.810000 600.000 1.75647 71.1996
Variable U L.C.size L.C.edge L.C.fract L.Crms TTL clstr	Jnit ha m - m N	s Mean 0.562500 405.000 1.57308 59.4908 800.833	St.Dev. 0.115925 81.4081 0.103942 5.77370 11.2802	C. V. 20.6089 20.1008 6.60753 9.70520 1.40856	Minimum 0.450000 300.000 1.40368 50.9117 781.000	Maximum 0.810000 600.000 1.75647 71.1996 817.000
Variable U L.C.size L.C.edge L.C.fract L.Crms TTL clstr TTL clstr	Jnit ha m - m N m	s Mean 0.562500 405.000 1.57308 59.4908 800.833 103765.	St.Dev. 0.115925 81.4081 0.103942 5.77370 11.2802 695.943	C. V. 20.6089 20.1008 6.60753 9.70520 1.40856 0.670691	Minimum 0.450000 300.000 1.40368 50.9117 781.000 102540.	Maximum 0.810000 600.000 1.75647 71.1996 817.000 104880.
Variable ( L.C.size L.C.edge L.C.fract L.Crms TTL clstr TTL clstr TTL edgs Sav size	Jnit ha m - m N m ha	s Mean 0.562500 405.000 1.57308 59.4908 800.833 103765. 0.125926	St.Dev. 0.115925 81.4081 0.103942 5.77370 11.2802 695.943 0.512321E-02	C. V. 20.6089 20.1008 6.60753 9.70520 1.40856 0.670691 4.06842	Minimum 0.450000 300.000 1.40368 50.9117 781.000 102540. 0.118870	Maximum 0.810000 600.000 1.75647 71.1996 817.000 104880. 0.135533
Variable U L.C.size L.C.edge L.C.fract L.Crms TTL clstr TTL edgs Sav size S_Freq	Jnit ha m m N m ha N	s Mean 0.562500 405.000 1.57308 59.4908 800.833 103765. 0.125926 929.833	St.Dev. 0.115925 81.4081 0.103942 5.77370 11.2802 695.943 0.512321E-02 1.11464	C. V. 20.6089 20.1008 6.60753 9.70520 1.40856 0.670691 4.06842 0.119875	Minimum 0.450000 300.000 1.40368 50.9117 781.000 102540. 0.118870 928.000	Maximum 0.810000 600.000 1.75647 71.1996 817.000 104880. 0.135533 932.000
Variable U L.C.size L.C.edge L.C.fract L.Crms TTL clstr TTL edgs Sav size S_Freq Cor_len	Jnit ha m m N m ha N m	AF Mean 0.562500 405.000 1.57308 59.4908 800.833 103765. 0.125926 929.833 36.3156	St.Dev. 0.115925 81.4081 0.103942 5.77370 11.2802 695.943 0.512321E-02 1.11464 1.57741	C. V. 20.6089 20.1008 6.60753 9.70520 1.40856 0.670691 4.06842 0.119875 4.34362	Minimum 0.450000 300.000 1.40368 50.9117 781.000 102540. 0.118870 928.000 34.5986	Maximum 0.810000 600.000 1.75647 71.1996 817.000 104880. 0.135533 932.000 40.1356

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