## QRULE

## A COMPUTER PROGRAM FOR LANDSCAPE HYPOTHESIS TESTING

developed by

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QRULE is an extension of RULE (Gardner 1999), a program for scale-dependent analysis of landscape patterns. The extensions provided in QRULE are designed to assist the user in the development and testing of alternative hypotheses relating the process of landscape change to the patterns observed. These differences may be statistically compared with a simple random pattern (i.e., the classical neutral model of Gardner et al. 1987), against an new model within QRULE, or by alternative models developed by the user.

This document provides a brief overview, focusing on the new features in Qrule. It is assumed that the reader has experience using RULE and is familiar with the concepts of neutral landscape models (Turner et al. 2001).

Program documentation, example input and output files, and the source code for Qrule may be obtained from www.al.umces.edu/QRULE. The Open Software License (http://www.opensource.org/licenses/index.php) applies to the distribution, use, and possible alteration of QRULE.

## OVERVIEW OF IMPROVEMENTS AND ADDITIONS

1. The output files generated by QRULE have been extensively revised and reformatted to assist in data display and statistical comparisons (see Table 1). Two new files, assmat.dat and arcgrid.map have been added. The association matrix among map cover types is statistically evaluated in assmat.dat, while arcgrid.map formats the first map iteration for display in ArcInfo.
2. The pattern metrics produced from map analysis are now expressed in metric units (i.e., in meters, hectares, etc.).
3. It is now possible, using the patch_cfd.dat data file to directly display the cumulative frequency distribution of patch sizes for each land-cover class. A program written in PERL is provided (cfdsum.pl) to illustrate how these plots may be performed.
4. The addition of alternative neutral models to QruLE is illustrated with the "mask" $<\mathrm{X}>$ option. This model is designed to test the hypothesis that landscape pattern is largely determined by dominant features (e.g., rivers, lakes, urban development) that constrain the patterns of other cover types. Adding additional options to QRULE is not difficult, but requires familiarity with Fortran 95 and the availability of a suitable compiler.

## Running Qrule

Input to QRULE may be either interactive or via file redirection. Each execution of QRULE requires the specification of: 1) the type of map to be generated and/or analyzed; 2) map characteristics; and 3) the output desired. Two types of input requests are illustrated below. The first is to analyze an existing map, while the second is to use the "masked" model for hypothesis testing. Blue text indicates output from Qrule while black text indicates user response.

First example: Analyze an input map

```
Qrule (v 4.1) Landscape Pattern Analysis
08/01/05
Enter map type to be analyzed:
            <I> Input existing map file
            <R> Generate a random map (with replacement)
            <S> Generate a simple random map
            <M> Generate a multifractal random map
            <G> Generate a multifractal random map with a gradient
            <X> Use input map as mask, random map for neutral model
```

i
Map choice: I
Enter name of input map file
rocr_reclass.map
Input map name: rocr_reclass.map
Enter number of map rows and columns (max $=2048$ ea.)
512512
Rows x Columns $=512 \times 512$
Enter the number of map classes
4
Map classes $=4$
Enter the neighborhood rule
1 - nearest neighbor ( $\mathrm{N} \_$n.b $=4$ )
2 - next nearest neighbor ( $N$ _nb = 8)
3 - 3rd nearest neighbor ( $N$ _ $\bar{n} b=12$ )
4 - user defined

1
Rule choice is: 1
Enter the number of replications
1
N_Reps = 1
Create an output maps?
$\mathrm{N}=$ None
$G=$ generated map
S = cluster Size map
C = cluster ID map
n
Map output choice $=\mathrm{N}$

```
Perform map analysis?
    <N>o analysis
    <L>acunarity analysis
    <R>ule analysis
    <A>ll (both Rule and Lacunarity)
```

r

```
Analysis method: RULE
What is the resolution of each grid element?
    (length of the side of a grid element, in meters)
```

Appendix A gives the results of this example in the 'rulerun.log' file.

## Second Example: Use the "mask" neutral model

This example requires two maps. The first map will be used to extract the land-cover adjacency matrix used in the neutral model. Bracketed text (in italics) has been inserted to clarify the purpose of some of the responses.

```
Qrule (v 4.1) Landscape Pattern Analysis 08/01/05
Enter map type to be analyzed:
            <I> Input existing map file
            <R> Generate a random map (with replacement)
            <S> Generate a simple random map
            <M> Generate a multifractal random map
            <G> Generate a multifractal random map with a gradient
            <X> Use input map as mask, random map for neutral model
```

x

```
    Map choice: X
    Enter number of map rows and columns (max = 2048 ea.)
512512
    Rows x Columns = 512 x 512
    Enter name of file to be used as a mask
rocr_reclass.map
    Input map name: rocr_reclass.map
    Enter number of cove\overline{r}}\mathrm{ types of the mask map
4
3
    Enter number of cover types for random generated maps
    {reclassification will be necessary}
    Cover types: mask = 4 random = 3
        Reclassify masked map
        Cover type 0 becomes ...
0 {the '0' class is a non-cover type - e.g., roads, etc.}
            Cover type 1 becomes ...
1
    Cover type 2 becomes ...
2
    Cover type 3 becomes ...
```

                Cover type 4 becomes ...
    from --> to
            00
            11
            22
            33
            40
    Type in the habitat type for the matrix
    set to zero to automatically select
            \{'1' is agriculture\}
    Background (matrix) \(=1\)
    Now we need the parameters for the
        random map cover types
    Enter a negative random number seed
    -1918171
Random number seed: -1918171
Enter the neighborhood rule
1 - nearest neighbor ( $N$ _n.b $=4$ )
2 - next nearest neighbōr ( $N$ _nb $=8$ )
3 - 3rd nearest neighbor ( N _̄̄b $=12$ )
4 - user defined

1

```
Rule choice is: 1
    Map classes = 3
    Enter the 4 probabilities, starting with p(0)
```

0
0.79955
0.19029
0.01015

The normalized probabilities are:

- P CumP
$0 \quad 0.0000 \quad 0.0000$
10.79960 .7996
$20.1903 \quad 0.9898$
$3 \quad 0.0102 \quad 1.0000$

Enter the number of replications
12
N_Reps = 12
Create an output maps?
$\mathrm{N}=$ None
$\mathrm{G}=$ generated map
$S$ = cluster Size map
C = cluster ID map
g
Map output choice $=$ G
Name of output file?
scratch.map

```
Output file for generated map: scratch.map
Perform map analysis?
    <N>o analysis
    <L>acunarity analysis
    <R>ule analysis
    <A>ll (both Rule and Lacunarity)
```

r
Analysis method: RULE
What is the resolution of each grid element?
(length of the side of a grid element, in meters)

See Appendix B for a listing of the entire input-output stream for this example.

## File redirection for batch-mode execution

Analysis projects often require multiple executions of QrULE. In these cases it will be convenient to use file redirection for input and output. In addition, the files produced by Qrule (Table X) will need to be renamed in order to prevent them from being overwritten (and thus destroyed) by subsequent program execution. If all the input responses are prepackaged in an input file (i.e., name.scriptfile) then QruLE can be run with a single line typed at the command prompt:

$$
\text { Qrule }<\text { name.scriptfile }>\text { output.save }
$$

Where 'QRULE' executes the program, the ' $<$ ' causes QRULE to read input from name.scriptfile and the ' $>$ ' causes screen output to be redirected to a file called output.save. Of course name.scriptfile and output.save are optional names for the files of your choice. Subsequent to execution, rulerun. log should be renamed to save the results and patch_cfd.dat renamed if summary statistics of patch sizes are desired.

Of course, multiple runs can be packaged into a batch file allowing unattended execution of multiple maps. This is most useful when the size maps and number of iterations are large.

Table 1. ASCII files that are used (I) or generated (G) by QruLE

| File name ${ }^{1}$ | Unit | Type | General description of contents |
| :---: | :---: | :---: | :---: |
| rulerun.log | 10 | G | log file of program input and simulation results |
| patch_cfd.dat | 11 | G | patch size frequency distribution for each map and habitat type. Output includes mean patch size, edge, radius mean square, and fractal for each patch size. |
| 'Idfile' | 12 | G | output map with each patch uniquely identified |
| 'sizefile' | 13 | G | name of output map with the patch sizes uniquely labeled |
| 'outfile' | 14 | G | name of output map with habitat types uniquely labeled |
| 'mapfile' | 15 | I | name of input map file for analysis by RULE |
| assmat.dat | 16 | G | matrix of neighbor association frequencies for each map |
| arcgrid.map | 19 | G | single map with header for input to ArcGrid for visualization and display |
| lacun.dat | 20 | G | output of lacunarity results |

${ }^{1}$ Single quoted names are specified by the user at runtime. Non-quoted names are invariant, being produced by each use of QRULE. The non-quoted file names should be renamed following each execution of QRULE to preserve program results.

Example input and output files are available at www.al.umces.edu/Qrule

## AddITIONAL FILES FOR PROCESSING DATA

The philosophy of the UNIX and LINUX operating systems is to increase programming efficiencies by linking programs with existing utilities via input-output files. Many of the statistical analyses that we have performed were accomplished by using existing plotting and statistical analysis software. Three PERL scripts, cfdsum.pl, compare.pl, and Qrule.pl, and a single fortran program, Kstest.f90, are provided (see otherstuff.zip) to aid the user in analyzing the output from Qrule. These files and programs are not documented here, but are offered to those with sufficient expertise to use and adapt to individual needs.

## Source code overview

The list of files required to compile QRULE, and the Makefile used to do so, are given in Table 2. Because Qrule uses advance features of Fortran 95, the Lahey compiler was used for both the DOS and LINUX versions (Lahey Computer Systems 1999). Most of the files listed in Table 2 contain multiple subroutines that are closely related to the functions listed.

Table 2 Program files for compilation and execution of QRULE

| File Name | File Type Purpose |
| :---: | :---: |
| Makefile | make recompile and update Fortran executable |
| Rule Executable |  |
| Qrule | Fortran executable <br> Available for DOS (Qrule.exe) and LINUX operating systems Fortran 95 Source Code |
| genmap.f90 | Subroutines for map generation |
| hfract.f90 | Multifractal map routine |
| input.f90 | Program input and control |
| lacun.f90 | Subroutine for optional output of lacunarity analysis (Plotnick et al. 1993). |
| main.f90 | Routine governing program execution |
| mapanal.f90 | Routines for map analysis |
| module.f90 | Defines variables and sets their dimensions |
| patchid.f90 | Routines for identification of landscape patches |
| ran1.f90 | Random number generation routine from Numerical Receipes (Press et al. 1992) |
| sizeit.f90 | Subroutines controlling the dynamic dimension of map variables |
| stats.f90 | Calculation and output of map statistics and indices |

Additional neutral models may be added to QRULE by:

1. Revising the input routine to accept the option of executing a different (additional) neutral model. The variable 'maptype' is used to identify the type of neutral model to generate. Code similar to that for the other map types will need to be added to this input file to recognize this new options and the parameters it may require.
2. The subroutine for the new neutral model should be added to the genmap.f90 file. In addition a call must be added to the GenMap routine (under 'select case (maptype)') in order for this new model to be linked with the Qrule code.
3. Recompile using Makefile

Obviously, the above is only an outline of the changes which may be required. Familiarity with fortran - or the ability to link programs written in other languages with this fortran code - are a prerequisite for making changes to QRULE.

## Metrics and statistics produced by Qrule

QRULE provides a set of landscape metrics that have proven to be helpful in understanding the effect of landscape fragmentation on pattern generation (Gardner 1999). Additional analyses may be achieved by exporting maps to ArcView or other programs such as Fragstats (McGarigal et al. 2002).

One new statistic has been added to QRULE: a chi-square test of the matrix of association of land-cover types. 'Chisquare', the subroutine performing this analysis, may be found in the file 'mapanalysis.f90.' There were 4 cover types in the examples listed in the appendices, with an association matrix that formed a $4 \times 4$ chisquare contingency table with 9 degrees of freedom (Zar 1996). The association matrix is listed in the examples in Appendix A and B includes the ' 0 ' cover class -regarded by Qrule as a "no data" class. Although these frequencies are listed, they were not a part of the chisquare test.

## Appendix A: Log file for first example

```
    Qrule (v 4.1) Landscape Pattern Analysis
                            08/01/05
    Map choice: I
    Input map name: rocr_reclass.map
    Rows x Columns = 512 x 512
    Map classes =
        4
    Rule choice is: 1
    N_Reps =
    Mäp output choice = N
    Analysis method: RULE
    Resolution: 30.0000 meters
    Mean Association Matrix
Avg_ChiX = 890910. w/ 9 df (%Xceed = 100.0000)
        0 1 2 3 4
        00.034900 0.001690 0.000614 0.000413 0.001469
        1 0.001690 0.204405 0.008997 0.000947 0.063994
        2 0.000614 0.008997 0.037996 0.000063 0.018968
        30.000413 0.000947 0.000063 0.001538 0.000593
        4 0.001469 0.063994 0.018968 0.000593 0.525662
p's 0.039086 0.280034 0.066639 0.003555 0.610686
STATISTICAL SUMMARY (N= 1; Resolution= 30.0000 meters)
--Cover Type 0 (non habitat)-- [p = 0.0391 Cum. p = 0.0391]
--Land Cover Type 1-- [p = 0.2800 Cum. p = 0.3191]
Variable Units Mean St.Dev. C. V. Minimum Maximum
    L.C.size ha 1152.45 0.00000 1.00000 1152.45 1152.45
    L.C.edge m 238320. 
    L.C.fract - 1.69101 m
```



```
    Sav size ha 495.711 0.00000 4 0.00000 495.711 495.711
    S_Freq N 73393.0 0.00000 0.00000 73393.0 73393.0
```



```
    Mer\overline{c}
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline Land Cove & er Ty & pe 2-- & [p & 0.0667 & \(\mathrm{p}=0\) & \\
\hline Variable U & Units & Mean & St. Dev. & C. V. & Minimum & Maximum \\
\hline L.C.size & ha & 88.5600 & 0.00000 & 0.00000 & 88.5600 & 88.5600 \\
\hline L.C.edge & m & 27780.0 & 0.00000 & 0.00000 & 27780.0 & 27780.0 \\
\hline L.C.fract & - & 1.74417 & 0.00000 & 0.00000 & 1.74417 & 1.74417 \\
\hline L.C. rms & m & 570.210 & 0.00000 & 0.00000 & 570.210 & 570.210 \\
\hline TTL Clstr & N & 3349.00 & 0.00000 & 0.00000 & 3349.00 & 3349.00 \\
\hline TTL edgs & m & 905160. & 0.00000 & 0.00000 & 905160. & 905160. \\
\hline Sav size & ha & 14.8859 & 0.00000 & 0.00000 & 14.8859 & 14.8859 \\
\hline S_Freq & N & 17484.0 & 0.00000 & 0.00000 & 17484.0 & 17484.0 \\
\hline Cor len & m & 435.873 & 0.00000 & 0.00000 & 435.873 & 435.873 \\
\hline Perc & \% & 0.00000 & 0.00000 & 0.00000 & 0.00000 & 0.00000 \\
\hline
\end{tabular}
\begin{tabular}{lllllll}
--Land Cover Type \(3--\) & & {\([p=\)} & 0.0036 & Cum. \\
Variable Units Mean & St.Dev. & C. V. & Minimum & Maximum \\
L.C.size ha & 6.93000 & 0.00000 & 0.00000 & 6.93000 & 6.93000 \\
L.C.edge m & 2400.00 & 0.00000 & 0.00000 & 2400.00 & 2400.00 \\
L.C.fract - & 1.51765 & 0.00000 & 0.00000 & 1.51765 & 1.51765
\end{tabular}
```

| L.C._rms | m | 204.194 | 0.00000 | 0.00000 | 204.194 | 204.194 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| TTL Clstr | N | 345.000 | 0.00000 | 0.00000 | 345.000 | 345.000 |
| TTL edgs | m | 63780.0 | 0.00000 | 0.00000 | 63780.0 | 63780.0 |
| Sav size | ha | 2.26522 | 0.00000 | 0.00000 | 2.26522 | 2.26522 |
| S_Freq | N | 934.000 | 0.00000 | 0.00000 | 934.000 | 934.000 |
| Cor_len | m | 169.501 | 0.00000 | 0.00000 | 169.501 | 169.501 |
| Perc | \% | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00000 |
| --Land Cover Type 4-- |  |  | P | 0.6107 | Cum. $\mathrm{p}=1.0000$ ] |  |
| Variable U | Uni | ts Mean | St.Dev. | C. V. | Minimum | Maximum |
| L.C.size | ha | 10208.3 | 0.00000 | 0.00000 | 10208.3 | 10208.3 |
| L.C.edge | m | $0.136008 \mathrm{E}+07$ | 0.00000 | 0.00000 | $0.136008 \mathrm{E}+07$ | $0.136008 \mathrm{E}+07$ |
| L.C.fract | - | 1.87103 | 0.00000 | 0.00000 | 1.87103 | 1.87103 |
| L.C._rms | m | 5419.64 | 0.00000 | 0.00000 | 5419.64 | 5419.64 |
| TTL Clstr | N | 2817.00 | 0.00000 | 0.00000 | 2817.00 | 2817.00 |
| TTL edgs | m | $0.270660 \mathrm{E}+07$ | 0.00000 | 0.00000 | $0.270660 \mathrm{E}+07$ | $0.270660 \mathrm{E}+07$ |
| Sav size | ha | 7656.26 | 0.00000 | 0.00000 | 7656.26 | 7656.26 |
| S_Freq | N | 160085. | 0.00000 | 0.00000 | 160085. | 160085. |
| Cor_len | m | 5303.52 | 0.00000 | 0.00000 | 5303.52 | 5303.52 |
| Perc | \% | 1.00000 | 0.00000 | 0.00000 | 1.00000 | 1.00000 |

## Appendix B: Log file for second example

```
    Qrule (v 4.1) Landscape Pattern Analysis 08/01/05
    Map choice: X
    Rows x Columns = 512 x 512
    File to use as mask: rocr_reclass.map
    Cover types: mask = 4 random = 3
    from --> to
        0
        1
        2 2
        3 3
        4 0
    Random number seed: -1918171
    Rule choice is: 1
    Map classes = 3
    The normalized probabilities are:
            P CumP
        0 0.0000 0.0000
        1 0.7996 0.7996
        2 0.1903 0.9898
        3 0.0102 1.0000
    N Reps = 12
    Mäp output choice = G
    Output file for generated map: scratch.map
    Analysis method: RULE
    Resolution: 30.0000 meters
    Using mask with ***** sites [p(0) = 0.64977]
            Mean Association Matrix
Avg_ChiX = 875462. w/ 5 df (%Xceed = 100.0000)
            0 1 1 2 3
        0 0.563500 0.083590 0.002552 0.000131
        1 0.083590 0.174154 0.020895 0.001571
        2 0.002552 0.020895 0.041427 0.001596
        30.0001310.001571 0.0015960.000249
p's 0.649772 0.280210 0.066471 0.003547
    STATISTICAL SUMMARY (N= 12; Resolution= 30.0000 meters)
--Cover Type 0 (non habitat)-- }\quad[p=0.6498 Cum. p = 0.6498]
--Land Cover Type 1-- [p = 0.2802 Cum. p = 0.9300]
\begin{tabular}{lllclll} 
Variable & Units & Mean & St. Dev. & C. V. & Minimum & Maximum \\
L.C.size & ha & 584.370 & 127.073 & 21.7453 & 360.810 & 785.340 \\
L.C.edge & m & 151230. & 46130.3 & 30.5034 & 95940.0 & 270300. \\
L.C.fract & 1.71680 & \(0.463942 \mathrm{E}-01\) & 2.70237 & 1.63812 & 1.77512 \\
L.C._rms & m & 1716.60 & 411.685 & 23.9826 & 1086.09 & 2777.87 \\
TTL Clstr & N & 7315.17 & 56.0062 & 0.765618 & 7232.00 & 7410.00 \\
TTL edgs & m & \(0.334782 \mathrm{E}+07\) & 13571.6 & 0.405384 & \(0.331752 \mathrm{E}+07\) & \(0.337638 \mathrm{E}+07\) \\
Sav size & ha & 123.546 & 28.0879 & 22.7347 & 80.3961 & 184.840 \\
S_Freq & N & 73462.9 & 7.04477 & \(0.958956 \mathrm{E}-02\) & 73450.0 & 73474.0 \\
Cor_len & m & 1439.29 & 346.311 & 24.0612 & 916.164 & 2255.83 \\
Perc & \(\%\) & 0.0000 & 0.0000 & 0.00000 & 0.00000 & 0.00000
\end{tabular}
--Land Cover Type 2-- [p = 0.0664 Cum. p = 0.9965]
\begin{tabular}{rlrrrr} 
Variable & Units Mean & St. Dev. & C. V. & Minimum & Maximum \\
L.C.size & ha & 56.9475 & 10.4017 & 18.2654 & 44.0100 \\
L.C.edge \(m\) & 18510.0 & 3574.78 & 19.3127 & 12960.0 & 24780.0
\end{tabular}
```

| L.C.fract | - | 1.68404 | 0.411394E-01 | 2.44290 | 1.63345 | 1.79039 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| L.C. rms | m | 497.870 | 52.2798 | 10.5007 | 382.026 | 580.443 |
| TTL $\overline{\mathrm{C}}$ lstr | N | 2219.58 | 81.1631 | 3.65668 | 2083.00 | 2403.00 |
| TTL edgs | m | 789545. | 16484.5 | 2.08784 | 758760 . | 831240 . |
| Sav size | ha | 14.8172 | 1.48497 | 10.0220 | 12.3929 | 17.9630 |
| S_Freq | N | 17418.2 | 5.00227 | $0.287186 \mathrm{E}-01$ | 17409.0 | 17431.0 |
| Cor len | m | 381.128 | 37.5106 | 9.84202 | 312.358 | 444.973 |
| Perc | \% | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00000 |
| --Land Cover Type 3-- |  |  | $[\mathrm{p}=$ | 0.0035 Cum. $\mathrm{p}=1.0000]$ |  |  |
| Variable | Unit | S Mean | St. Dev. | C. V. | Minimum | Maximum |
| L.C.size | ha | 0.562500 | 0.115925 | 20.6089 | 0.450000 | 0.810000 |
| L.C.edge | m | 405.000 | 81.4081 | 20.1008 | 300.000 | 600.000 |
| L.C.fract | - | 1.57308 | 0.103942 | 6.60753 | 1.40368 | 1.75647 |
| L.C._rms | m | 59.4908 | 5.77370 | 9.70520 | 50.9117 | 71.1996 |
| TTL clstr | N | 800.833 | 11.2802 | 1.40856 | 781.000 | 817.000 |
| TTL edgs | m | 103765. | 695.943 | 0.670691 | 102540. | 104880. |
| Sav size | ha | 0.125926 | $0.512321 \mathrm{E}-02$ | 4.06842 | 0.118870 | 0.135533 |
| S_Freq | N | 929.833 | 1.11464 | 0.119875 | 928.000 | 932.000 |
| Corr_len | m | 36.3156 | 1.57741 | 4.34362 | 34.5986 | 40.1356 |
| Perc | \% | 0.00000 | 0.00000 | 0.00000 | 0.00000 | 0.00000 |

## References

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